# **DIS and Hadronization systematic errors**

- 0. Introduction
- 1. DIS Bodek-Yang parameterization
- 2. DIS differential cross section error
- 3. DIS A-scaling error
- 4. DIS PDF error
- 5. Low-W hadronization error
- 6. High-W hadronization error
- 7. Conclusion

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Teppei Katori and Shivesh Mandalia NuWro Workshop, Dec. 3, 2017

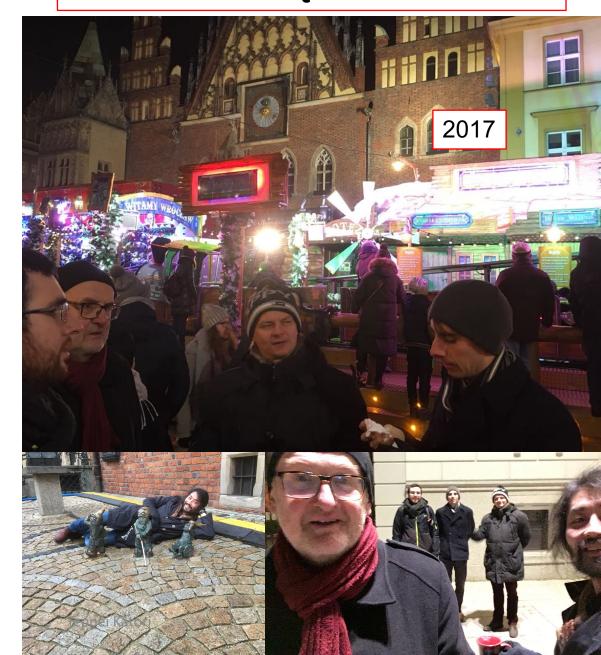
Teppei Katori

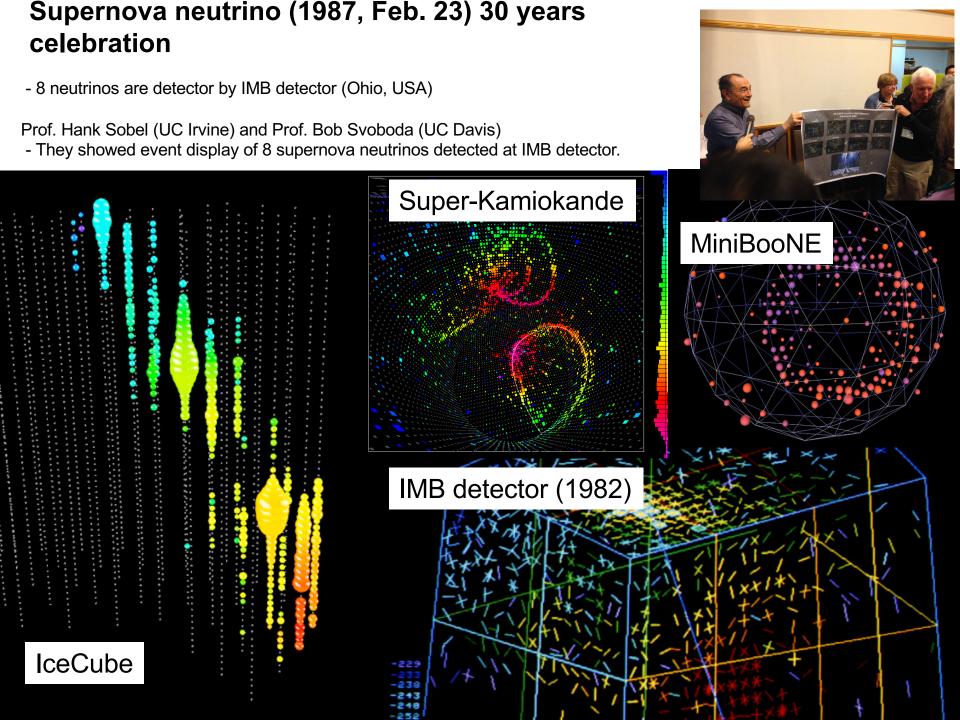
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# Kochom cię, Wrocław!

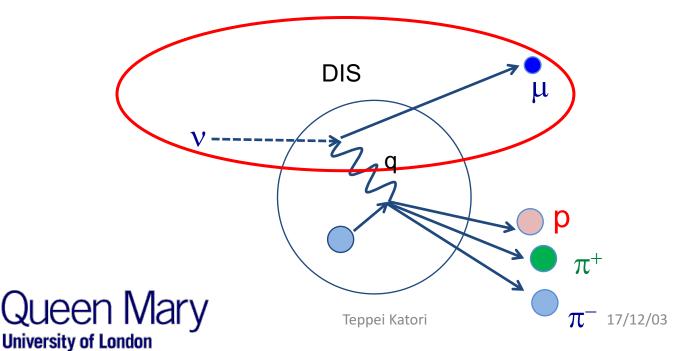




#### 0. Neutrino cross section overview

#### Deep Inelastic Scattering (DIS)

- a process to scatter a charged lepton by an incident lepton with given energy
- DIS differential cross section is function of x and y
- DIS total cross section is function of Ev, integrated in x and y



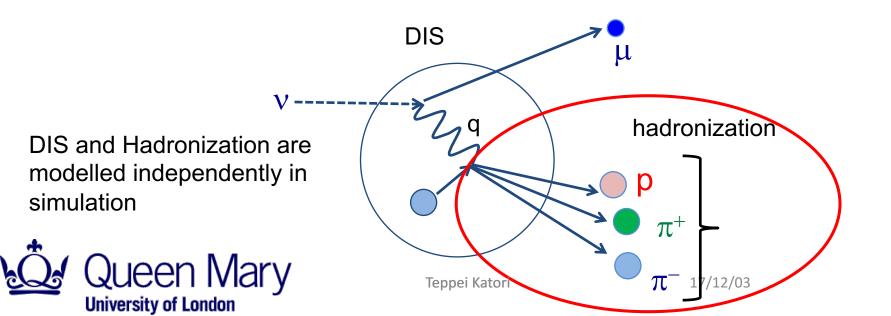
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#### Hadronization

- Hadronization is a process to generate hadrons from given Q<sup>2</sup> and W
- number of hadrons (multiplicity) and hadrons kinematics are computed.



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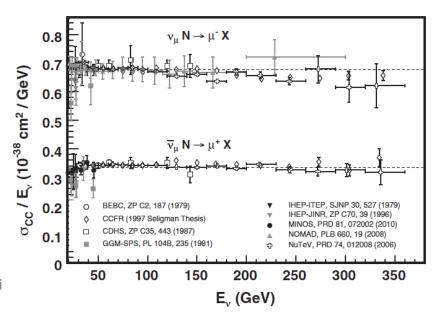
- Hadronization is a process to generate hadrons from given Q<sup>2</sup> and W
- number of hadrons (multiplicity) and hadrons kinematics are computed.

$$-\sigma(v)/E = 0.677 \pm 0.014 \times 10^{-38} \text{ (cm}^2/\text{GeV)}$$

#### DIS total cross section error ~ 2%?

- This is the error of CCDIS total cross section at 30 to 200 GeV
- Most of our analyses need errors of differential cross section error

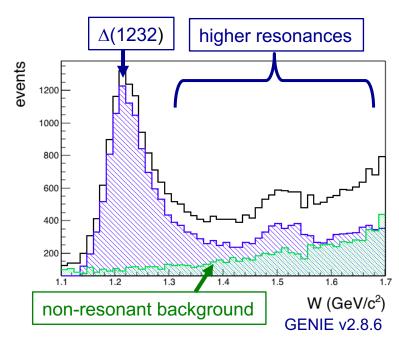




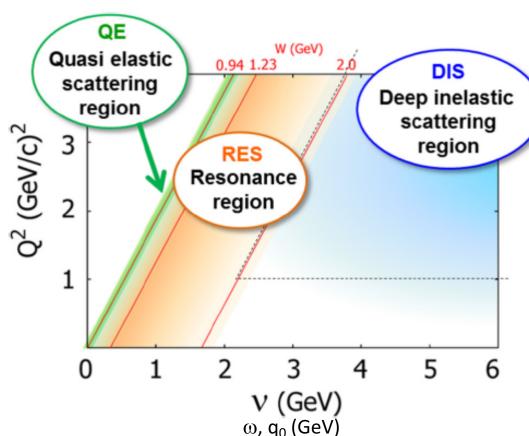
# 0. SIS region physics

#### **Basic ingredients**

- $\Delta$ (1232)-resonance
- higher resonances
- non-resonant background



#### Rep. Prog. Phys. 80 (2017) 056301



**Figure 1.** Kinematical regions of the neutrino-nucleus interaction relevant to the next-generation neutrino-oscillation experiments. The energy transfer to a nucleus and the squared four-momentum transfer are denoted by  $\nu$  and  $Q^2$ , respectively.



# 0. GENIE SIS model

Cross section

W<sup>2</sup><2.9 GeV<sup>2</sup>: RES

W<sup>2</sup>>2.9 GeV<sup>2</sup> : DIS

Hadronization

W<sup>2</sup><5.3GeV<sup>2</sup>: KNO scaling based model

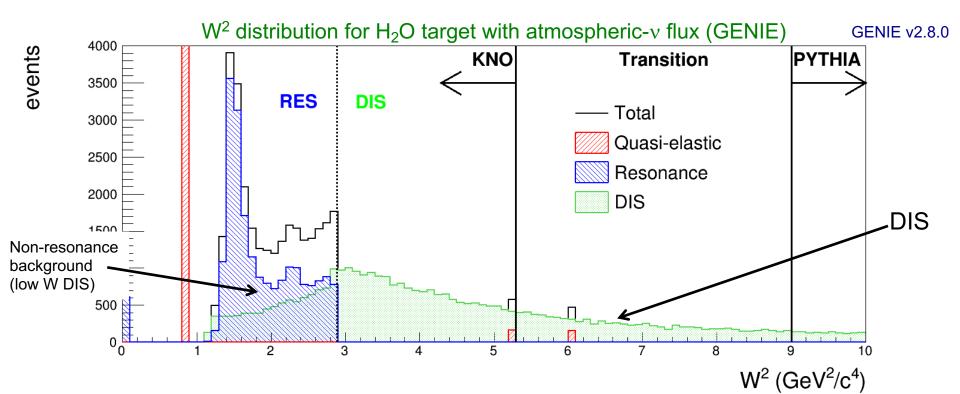
 $2.3 \text{GeV}^2 < \text{W}^2 < 9.0 \text{GeV}^2$ : transition

9.0GeV<sup>2</sup><W<sup>2</sup>: PYTHIA6

There are 2 kind of "transitions" in SIS region

- cross-section

- hadronization



#### 0. NEUT SIS model

**Cross section** 

 $W^2$ <4 GeV<sup>2</sup> : RES  $W^2$ >4 GeV<sup>2</sup> : DIS

Hadronization

W<sup>2</sup><4GeV<sup>2</sup>: KNO scaling based model

4GeV<sup>2</sup><W<sup>2</sup>: PYTHIA5

University of London

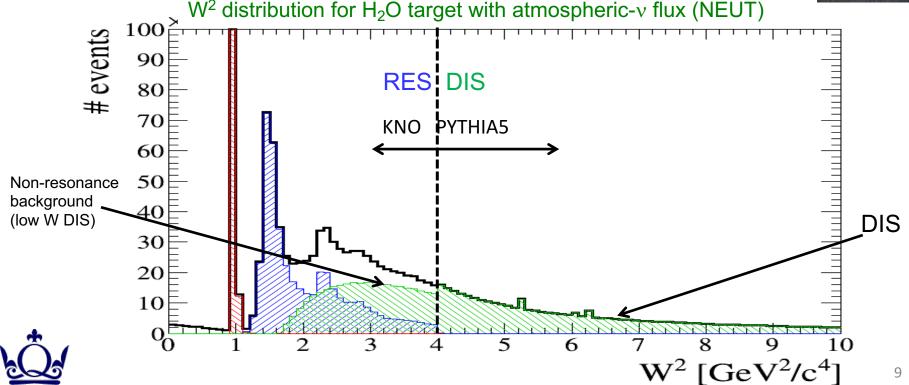
There are 2 kind of "transitions" in SIS region

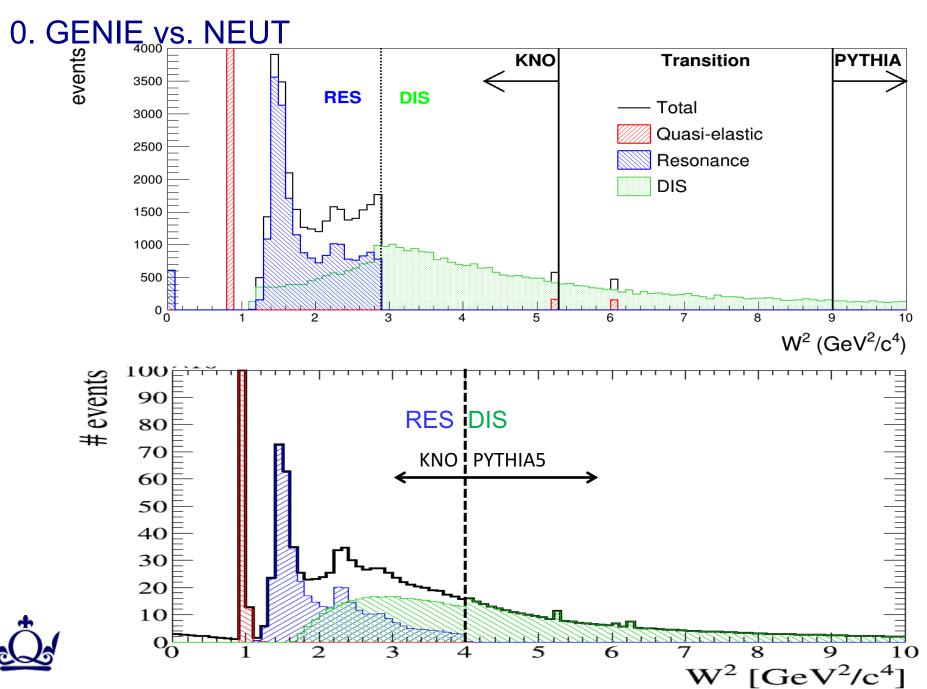
- cross-section

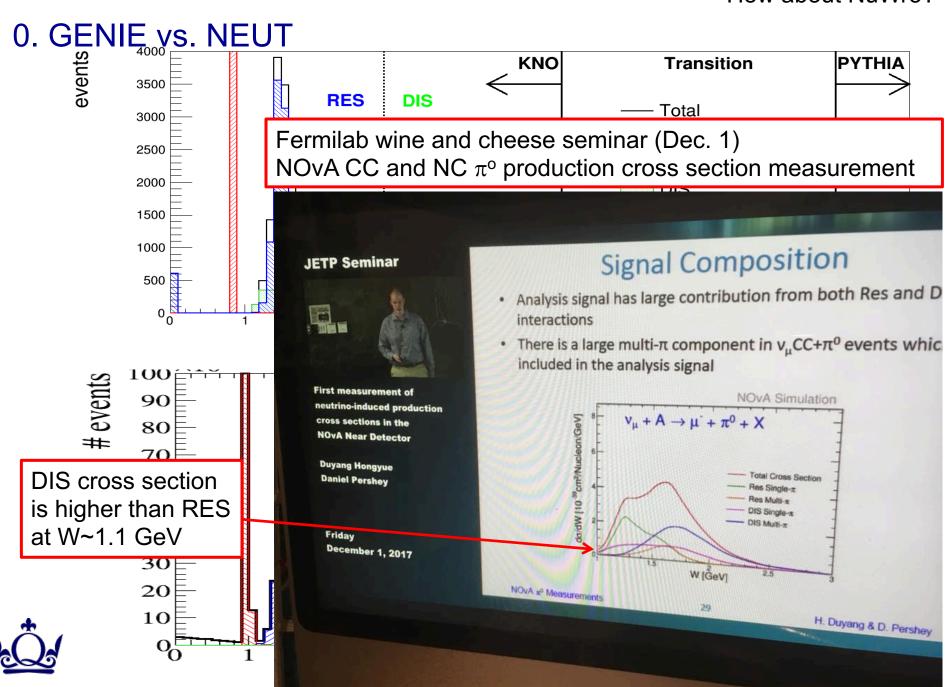
- hadronization

Christophe Bronner (IPMU)









### 0. DIS-hadronization error check list

- Goal is to make event weight with function of Ev, x, y, etc, for IceCube oscillation program
- All errors are expected to be unimportant (?)

DIS or Hadronization	type of error	approach	size
DIS	Bodek-Yang correction	play with Bodek-Yang parameters (by eyes)	????
DIS	differential xs	NuTeV-GENIE comparison (bottom-up)	????
DIS	A-scaling	MINERvA-GENIE (bottom-up)	????
DIS	PDF	From nuclear PDF, CT10? nCTEQ? (top-down)	????
Hadronization	low W averaged charged hadron multiplicity	play with KNO parameters (by eyes)	????
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### 0. Introduction

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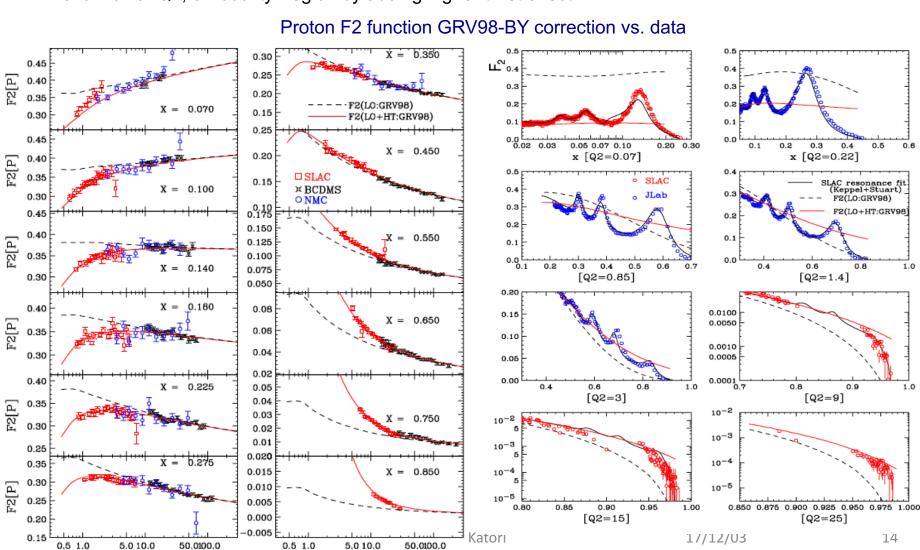


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# 1. Bodek-Yang correction for low Q<sup>2</sup> DIS

Q2

GRV98 is a PDF designed for low Q2 region. Bodek-Yang correction makes GRV98 to work even lower Q2, or "duality" region by adding higher twist effect



Q2

Nachtmann  $\xi = \frac{2x}{\left(1 + \sqrt{1 + \frac{4x^2M^2}{Q^2}}\right)}$ 

# 1. Bodek-Yang correction for low Q<sup>2</sup> DIS

In GENIE, there are 11 parameters to control "Bodek-Yang correction" on GRV98 LO PDF

- A: high order twist correction
- B: quark transverse momentum
- Cvu1, Cvu2: valence u-quark PDF correction
- Cvd1, Cvd2: valence d-quark PDF correction
- Cs1u, Cs1d: sea u- and d-quark PDF correction
- x0, x1, x2: d(x)/u(x) correction

		impact (%)		
	parameter	1  year	3 year	5 year
	hierarchy	100.0	100.0	100.0
	$\Delta m^2_{31}$	38.8	37.9	37.6
	Energy scale	21.2	21.4	21.7
	$A_{eff}$ scale	15.2	13.2	11.4
	$ heta_{23}$	3.4	4.8	5.7
	$\nu_{\rm e}/numu$ ratio	0.5	1.7	2.6
	$nu/\overline{\nu}$ ratio	0.5	1.2	2.3
	$M_A^{RES}$	1.2	2.0	1.7
	$C_{V1u}^{BY}$	0.1	0.3	0.3
	$C_{V2u}^{BY}$	0.0	0.0	0.2
DIS errors	$\theta_{13}$	0.0	0.1	0.2
	$A_{HT}^{BY}$	0.0	0.0	0.0
	$M_A^{CCQE}$	0.0	0.0	0.0
	$B_{HT}^{BY}$	0.0	0.0	0.0

$$\xi \to \xi_{\omega} = \frac{2x\left(1 + \frac{M_f^2 + B}{Q^2}\right)}{\left(1 + \sqrt{1 + \frac{4x^2M^2}{Q^2}}\right) + \frac{2Ax}{Q^2}}$$

$$K_{valence}(Q^{2}) = [1 - G_{D}^{2}(Q^{2})] \cdot \left(\frac{Q^{2} + C_{v2}}{Q^{2} + C_{v1}}\right)$$
$$K_{sea}(Q^{2}) = \frac{Q^{2}}{Q^{2} + C_{s1}}$$

#### **PINGU LoI variations**

nominal value	uncertainty (%)	
0.99	-15, +25	
1.120	$\pm 20$	
0.538	$\pm 25$	
0.305	$\pm 25$	
0.291	$\pm 30$	
0.189	$\pm 30$	
	0.99 1.120 0.538 0.305 0.291	



# 1. Bodek-Yang correction errors

Parameter variations are defined

- errors A and B: I follow Joshua's choice
- errors on PDF correction: 30% for all
- errors on d(x)/u(x): next page

BY- parameters	CV	error	
Α	0.538	±25%	
В	0.305	±25%	
CsU	0.363	±30%	
CsD	0.621	±30%	
Cv1U	0.291	±30%	
Cv2U	0.189	±30%	
Cv1D	0.202	±30%	
Cv2D	0.255	±30%	
X0	-0.00817	+0.00817	
X1	0.0506	-0.0506	
X2	0.0798	-0.0798	atori

Since no correlations of parameters are available, 9 BY-systematic study samples are made to maximize of parameter variation effects

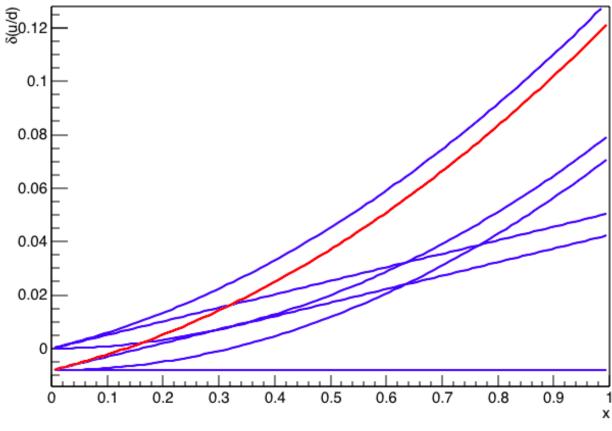
sample	sample
1	default
2	$A+\delta A$ , $B-\delta B$
3	A- $\delta$ A, B+ $\delta$ B
4	CsU+δCsU, CsD-δCsD
5	CsU-δCsU, CsD+δCsD
6	Cv1U+δCv1U, Cv2U-δCv2U
7	Cv1U-δCv1U, Cv2U+δCv2U
8	Cv1D+δCv1D, Cv2D-δCv2D
9	Cv1D-δCv1D, Cv2D+δCv2D
10	X0=0, X1=0, X2=0

# 1. d(x)/u(x) variation study

$$\delta(d(x)/u(x)) = X0 + X1^*x + X2^*x^2$$

- 2<sup>nd</sup> order polynomial describe this error, ~10% effect at large x
- A reasonable choice of envelope is when the function is 0.

BY u/d ratio correction, 0.05<x<0.75

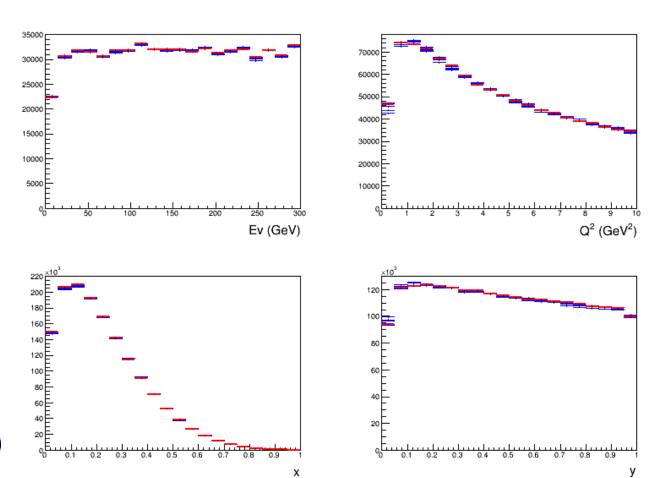




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# 1. Results

BY parameter variation make small variations in Ev, Q2, x, y.



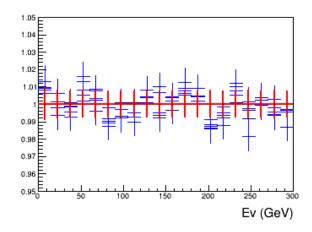


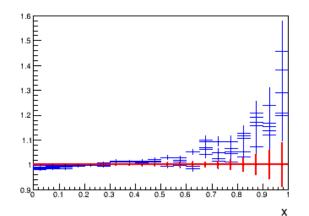
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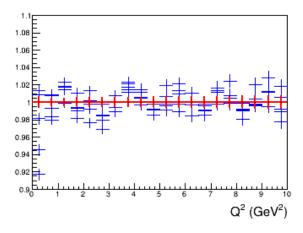
BY parameter variation make small variations in Ev. Q2, x, y.

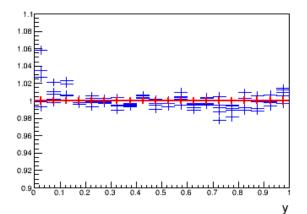
- Ev: <2% variation in all region
- Q2: ~8% variation at Q2=0.5 GeV2
- x: ~50% variation at x~1
- y: ~6% variation at y~0

In general, variation can be large by assuming correlations on parameters











# 1. DIS Bodek-Yang correction error

- Goal is to make event weight with function of Ev, x, y, etc, for IceCube oscillation program
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DIS or Hadronization	type of error	approach	size
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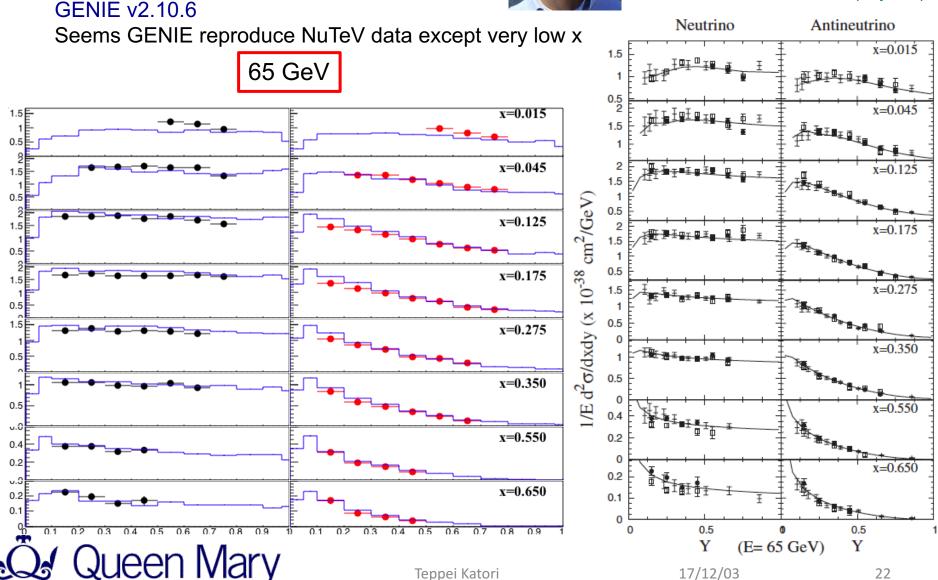
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# 2. GENIE-NuTeV comparison



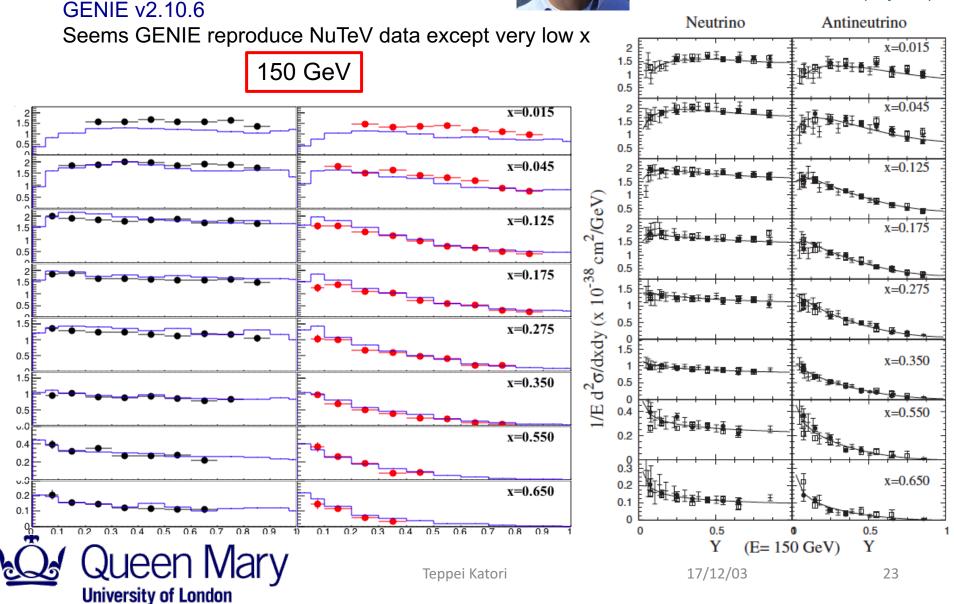
NuTeV v-Fe and antiv-Fe differential cross section (x, y, Ev)



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NuTeV v-Fe and antiv-Fe differential cross section (x, y, Ev)



**University of London** 

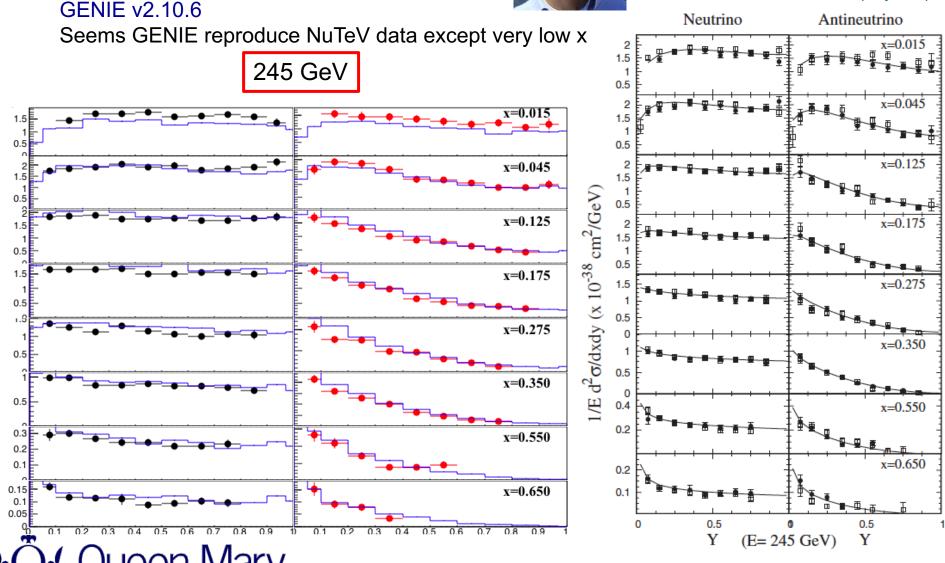
# 2. GENIE-NuTeV comparison



NuTeV v-Fe and antiv-Fe differential cross section (x, y, Ev)

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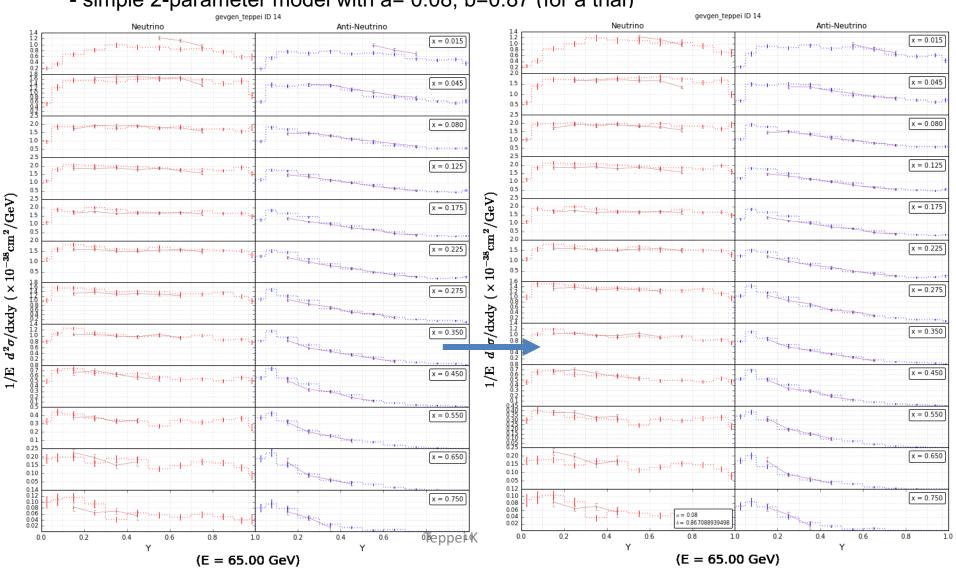
Teppei Katori

# 2. DIS differential cross section error

$$F(x,y) = bx^{-a}$$

#### **GENIE-NuTeV** comparison

- simple 2-parameter model with a= 0.08, b=0.87 (for a trial)

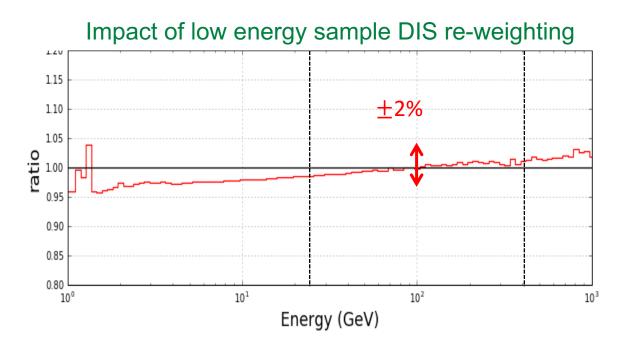


### 2. DIS differential cross section error

$$F(x,y) = bx^{-a}$$

#### **GENIE-NuTeV** comparison

- simple 2-parameter model with a= 0.08, b=0.87 (for a trial)
- it has 2-3% shift of energy spectrum in 30-200 GeV
- However, the shift (~error) is larger than ±2% at <10GeV and >300 GeV





### 2. DIS differential cross section error

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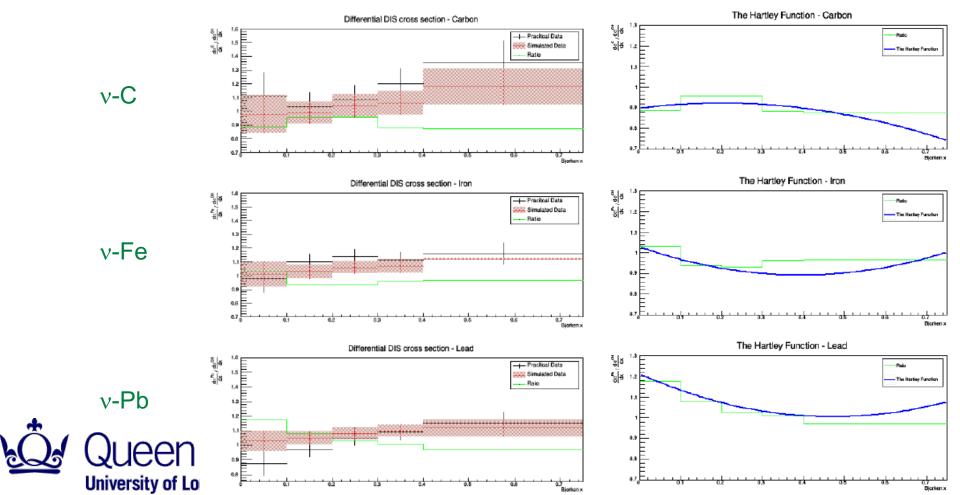
# 3. DIS A-dependent error

#### **GENIE-MINERvA** comparison

- $\frac{d\sigma^A}{dx} / \frac{d\sigma^{CH}}{dx} = \frac{10A}{(-0.0084A^2 + 9.9A + 16)} + \frac{0.95(15 A)}{A}x + \frac{0.95(A 13.25)}{(A 10)}x^2$
- Make a polynomial scaling function in A from data-MC ratio.
- Weight GENIE with function of x
- Bottom-up A-dependent DIS correction in x



Liam Hartley (Queen Mary)



# 3. DIS A-dependent error

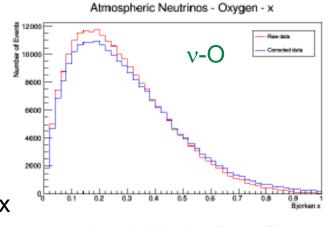
#### **GENIE-MINERvA** comparison

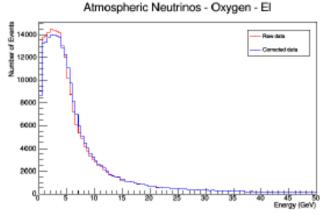
$$\frac{d\sigma^{A}}{dx} / \frac{d\sigma^{CH}}{dx} = \frac{10A}{(-0.0084A^{2} + 9.9A + 16)} + \frac{0.95(15 - A)}{A}x + \frac{0.95(A - 13.25)}{(A - 10)}x^{2}$$

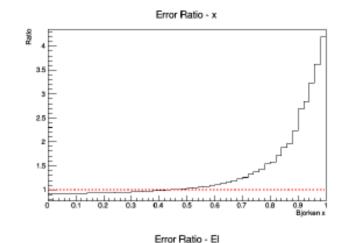
- Make a polynomial scaling function in A from data-MC ratio.
- Weight GENIE with function of x
- Bottom-up A-dependent DIS correction in x
- Make prediction of correction in any targets, for example oxygen

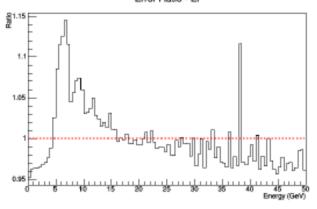
Reasonably large variation (~10-20%) in x (under investigation)

University of London









# 3. DIS A-dependent error

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- All errors are expected to be unimportant (?)

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### 4. DIS PDF error

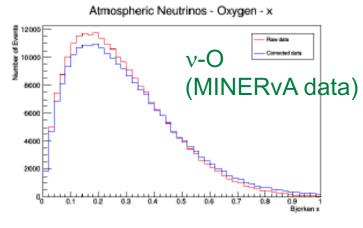
a

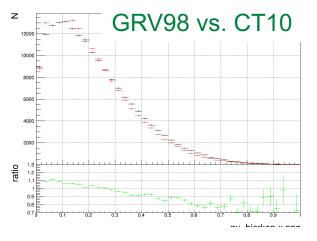
We tried to use couple of PDF from LHA PDF

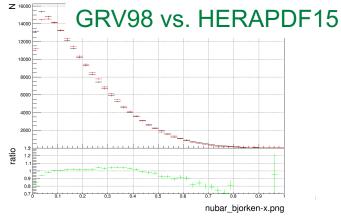
- CT10 (NLO)
- HERAPDF15 (NLO)
- NNPDF23 (NLO)

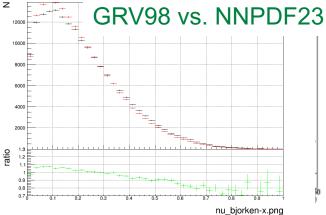
As expected(?), PDF variation (top-down error) is smaller and well-controlled.

→ If we use a better PDF, variation would be few %











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DIS	A-scaling	MINERvA-GENIE (bottom-up)	maybe large?
DIS	PDF	From nuclear PDF, CT10? nCTEQ? (top-down)	expected to be tiny
Hadronization	low W averaged charged hadron multiplicity	play with KNO parameters (by eyes)	????
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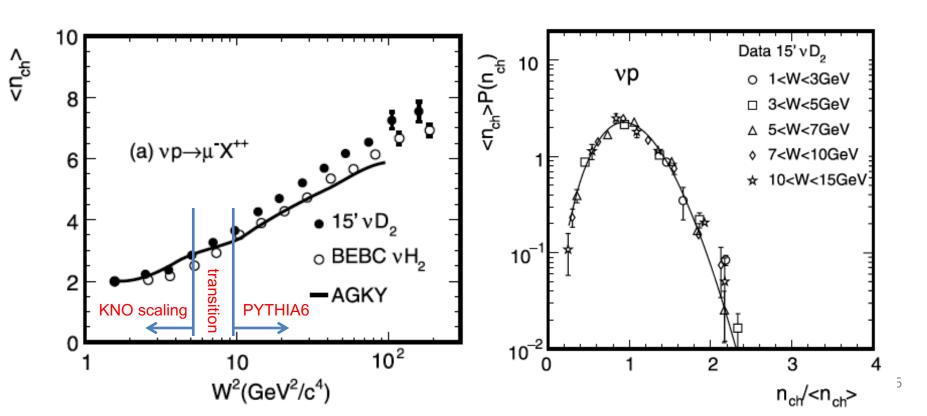
### 5. Low-W hadronization model

In AGKY model, hadronization model is a combination of 2 models.

#### KNO-scaling based model (low W hadronization)

- Data-driven model (agree with bubble chamber data, by construction)  $\langle n_{ch} \rangle = a_{ch} + b_{ch} \cdot \ln(W^2)$
- Averaged charged hadron multiplicity <n<sub>ch</sub>> is chosen from data, with empirical function
- Averaged neutral hadron multiplicity is chosen from isospin.
- Then variance of multiplicity is chosen from KNO-scaling law.

$$\langle n \rangle \cdot P(n) = \frac{2e^{-c}c^{cn/\langle n \rangle + 1}}{\Gamma(cn/\langle n \rangle + 1)}$$



TK and Mandalia, JPhysG42(2015)115004, arXiv:1602.00083

### 5. Low-W hadronization model

I added ±25% variation on "b<sub>ch</sub>" parameters

→ This imitate discontinuity of hadron multiplicity

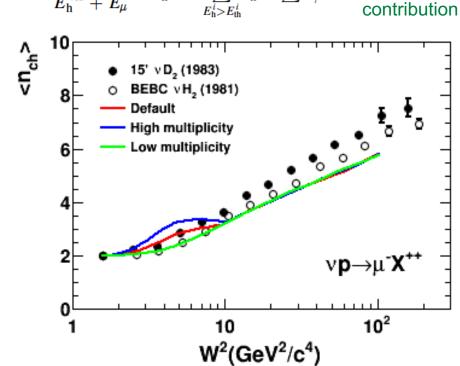
It looks to cover existing data variation

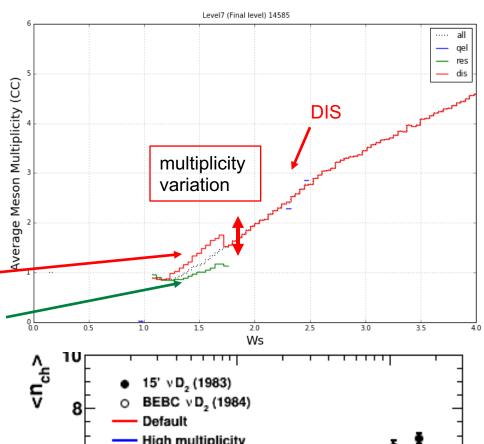
Then translate this variation in terms of hadron visible energy

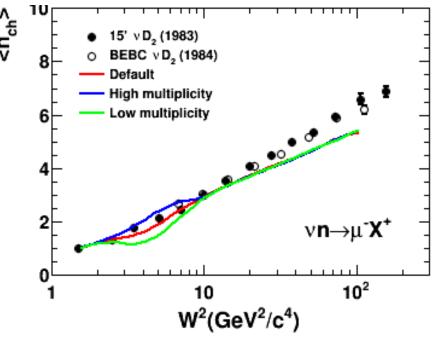
visible energy non-resonance background

resonance

$$y^{
m eff} = rac{E_{
m h}^{
m vis}}{E_{
m h}^{
m vis} + E_{\mu}} \cdot \quad E_{
m h}^{
m vis} = \sum_{E_{
m h}^i > E_{
m th}^i} T_{
m h}^i + \sum E_{\gamma}^i.$$







0.9

8.0

1000

#### 5. Low-W hadronization error

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Teppei Katori 17/12/03

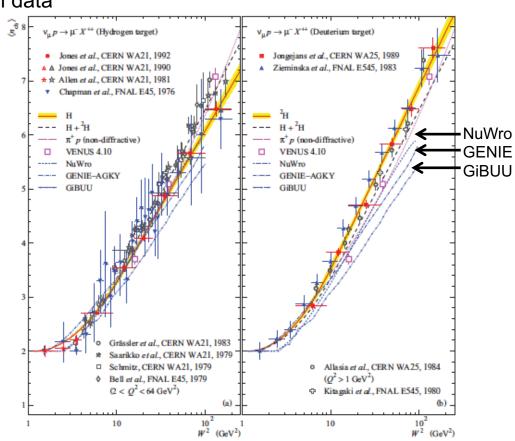
40

### 6. High-W hadronization model

#### Kuzmin-Naumov fit

- They systematically analysed all bubble chamber data
  - Difference of hydrogen and deuterium data
  - Presence of kinematic cuts
  - Better parameterization

All PYTHIA-based models underestimate averaged charged hadron multiplicity data (GiBUU, GENIE, NuWro, NEUT)



Average charged hadron multiplicity with function of W<sup>2</sup>

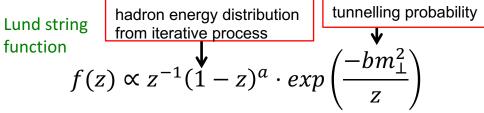


Sketch of fragmentation from  $q - \bar{q}$  string breaking

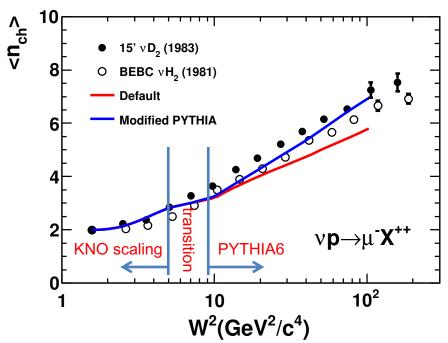
### 6. High-W hadronization model

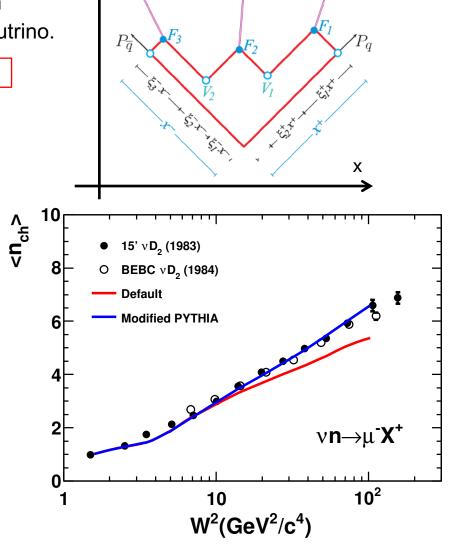


- PYTHIA6 with tuned Lund string function can reproduce <n<sub>ch</sub>> data both neutrino and antineutrino.



Neutrino average charged hadron multiplicity







### 6. High-W hadronization model error

#### Averaged charged hadron multiplicity <n<sub>ch</sub>>

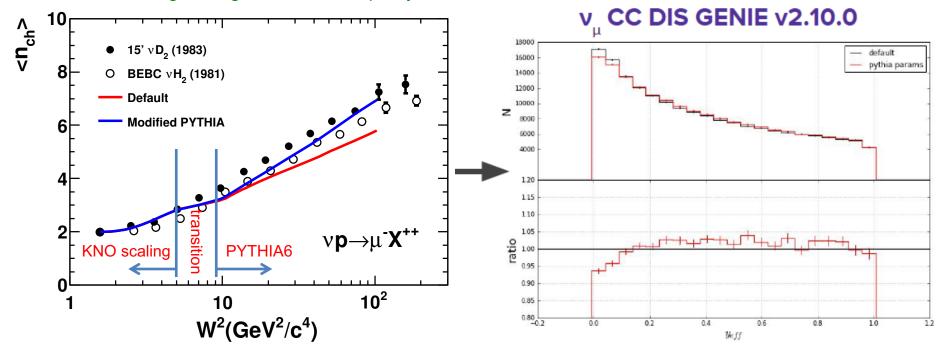
- PYTHIA6 with tuned Lund string function can reproduce <n<sub>ch</sub>> data both neutrino and antineutrino.

$$E_{\mathrm{h}}^{\mathrm{vis}} = \sum_{E_{\mathrm{h}}^{i} > E_{\mathrm{h}}^{i}} T_{\mathrm{h}}^{i} + \sum E_{\gamma}^{i}.$$
 
$$y^{\mathrm{eff}} = \frac{E_{\mathrm{h}}^{\mathrm{vis}}}{E_{\mathrm{h}}^{\mathrm{vis}} + E_{\mu}}.$$

#### Hadronization error propagation

- Difference of averaged charged hadron multiplicity is translated to visible hadron energy, then effective inelasticity. This is applied to variation of inelasticity error in simulation. Impact of hadronization error is small for experiments which only measure hadron shower

Neutrino average charged hadron multiplicity

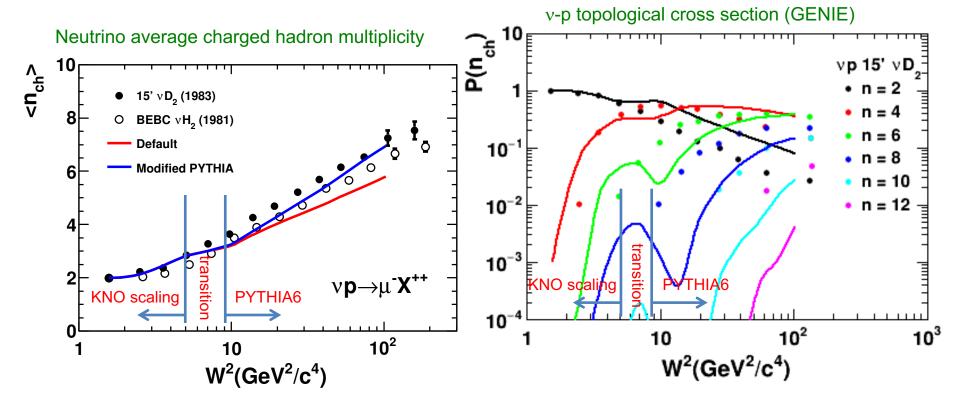


### 6. High-W hadronization dispersion error?

#### Bubble chamber topological cross section data

Although averaged charged hadron multiplicity makes continuous curve, topological cross sections are discontinuous, because multiplicity dispersion by PYTHIA6 is much narrower than bubble chamber data.

If the experiment is sensitive to hadron counting, you need to re-think how to propagate hadronization error...



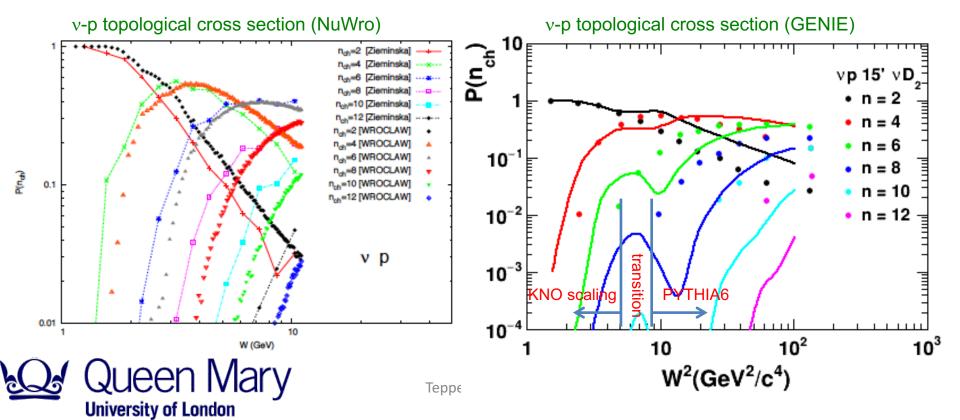


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### 7. DIS-hadronization errors, summary

- Goal is to make event weight with function of Ev, x, y, etc, for IceCube oscillation program
- Some of systematic errors are identified to be dangerous

	DIS or Hadronization	type of error	approach	size
some study (MSU)	DIS	Bodek-Yang correction	play with Bodek-Yang parameters (by eyes)	maybe large?
done	DIS	differential xs	NuTeV-GENIE comparison (bottom-up)	1-2% by GENIE study
under investigatio	DIS n	A-scaling	MINERvA-GENIE (bottom-up)	maybe large?
some study (MSU)	DIS	PDF	From nuclear PDF, CT10? nCTEQ? (top-down)	expected to be tiny
under investigatio	Hadronization n	low W averaged charged hadron multiplicity	play with KNO parameters (by eyes)	maybe large?
done JPhysG42(20	Hadronization	high W averaged charged hadron multiplicity	bubble chamber-PYTHIA comparison (bottom-up)	1-2% by GENIE study



#### 7. Conclusion

- Goal is to make event weight with function of Ev, x, y, etc, for IceCube oscillation program
- Some of systematic errors are identified to be dangerous

Bodek-Yang correction: We must update it in the near future. It is out-of-date, and systematic error estimation is impossible.

DIS differential cross section error: Systematic error is under control.

DIS A-dependent error: It may be large, need a careful study. MINERvA data is a starting point but a dedicated argon-DIS cross section measurement may remove this error (NuMI beam at SBN?)

DIS PDF error: It looks error can be estimated easily.

Low W hadronization error: It may be large, need a careful study. Incoherent treatment of resonances (RES) and non-resonant background (DIS) may be a problem.

High W hadronization error: Systematic error is under control.

## Thank you for your attention!



# Back up



#### 1. Neutrino cross section overview

GENIE uses "Frankenstein" model..., there are 2 transtions for both cross section and hadronization

**Cross section** 

W<sup>2</sup><2.9 GeV<sup>2</sup>: RES

W<sup>2</sup>>2.9 GeV<sup>2</sup> : DIS

Hadronization (AGKY model)

W<sup>2</sup><5.3GeV<sup>2</sup>: KNO scaling based model

 $5.3 \text{GeV}^2 < \text{W}^2 < 9.0 \text{GeV}^2$ : transition

9.0GeV<sup>2</sup><W<sup>2</sup>: PYTHIA6

